

The Limit of a Function 1

Problem 1: Sketch the graph of a function f with the given properties:

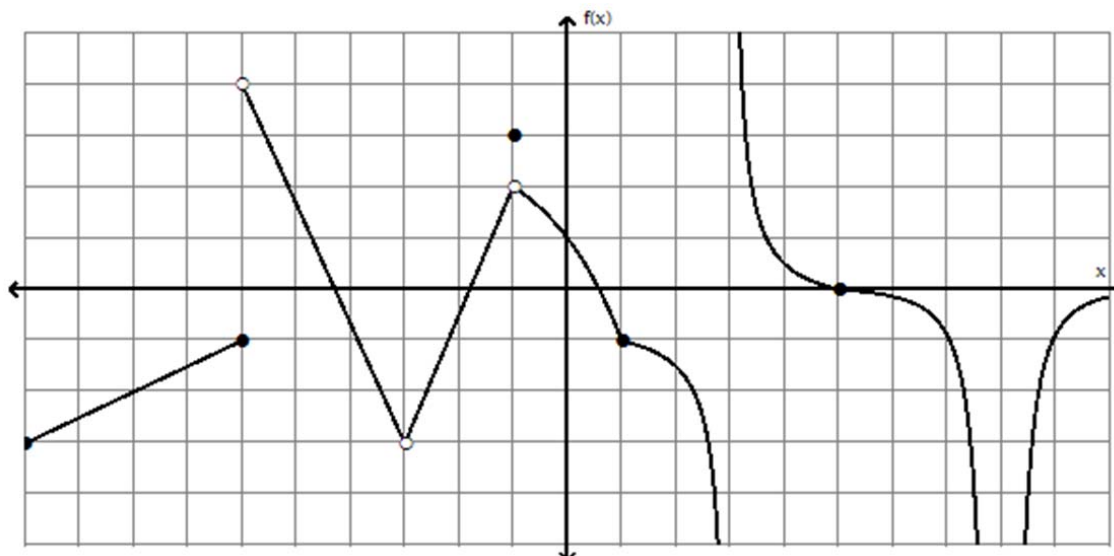
$$\lim_{x \rightarrow 3} f(x) = 5, \quad \lim_{x \rightarrow \infty} f(x) = 0, \quad \lim_{x \rightarrow -2} f(x) = -3, \quad \text{and} \quad \lim_{x \rightarrow -\infty} f(x) = 0.$$

Problem 2: Sketch the graph of a function f with the given properties:

$$\lim_{x \rightarrow -\infty} f(x) = 0, \quad \lim_{x \rightarrow -1^-} f(x) = -\infty, \quad \lim_{x \rightarrow -1^+} f(x) = \infty, \quad \lim_{x \rightarrow 0} f(x) = f(0), \quad f(0) = 1, \quad \lim_{x \rightarrow \infty} f(x) = 4$$

Introduction To Limits

Name _____



Use the graph above to evaluate each limit, or if appropriate, indicate that the limit does not exist.

1. $\lim_{x \rightarrow -6^-} f(x)$

2. $\lim_{x \rightarrow -6^+} f(x)$

3. $\lim_{x \rightarrow -6} f(x)$

4. $\lim_{x \rightarrow -3^+} f(x)$

5. $\lim_{x \rightarrow -3} f(x)$

6. $\lim_{x \rightarrow -1^-} f(x)$

7. $\lim_{x \rightarrow -1^+} f(x)$

8. $\lim_{x \rightarrow -1} f(x)$

9. $\lim_{x \rightarrow 1} f(x)$

10. $\lim_{x \rightarrow 3^-} f(x)$

11. $\lim_{x \rightarrow 3^+} f(x)$

12. $\lim_{x \rightarrow 3} f(x)$

13. $\lim_{x \rightarrow 8^+} f(x)$

14. $\lim_{x \rightarrow 8} f(x)$